

## MA 114 Worksheet #21: Centers of Mass

1. Find the center of mass for the system of particles of masses 4, 2, 5, and 1 located at the coordinates  $(1, 2)$ ,  $(-3, 2)$ ,  $(2, -1)$ , and  $(4, 0)$ .
2. Point masses of equal size are placed at the vertices of the triangle with coordinates  $(3, 0)$ ,  $(b, 0)$ , and  $(0, 6)$ , where  $b > 3$ . Find the center of mass.
3. Find the centroid of the region under the graph of  $y = 1 - x^2$  for  $0 \leq x \leq 1$ .
4. Find the centroid of the region under the graph of  $f(x) = \sqrt{x}$  for  $1 \leq x \leq 4$ .
5. Find the centroid of the region between  $f(x) = x - 1$  and  $g(x) = 2 - x$  for  $3/2 \leq x \leq 2$ .

## MA 114 Math Excel Worksheet #21: Centers of Mass

1. Determine the center of mass for the region bounded by  $y = 2 \sin(2x)$ ,  $y = 0$ ,  $x = 0$ , and  $x = \pi/2$ .
2. Determine the center of mass for the region bounded by  $y = x^3$  and  $y = \sqrt{x}$ .
3. Find the centroid of the region bounded by  $y = 3 + \sqrt{4 - x^2}$ ,  $y = 0$ ,  $x = -2$  and  $x = 2$ .
4. Find the centroid of the region bounded by  $y = 0$  and  $y = b\sqrt{1 - x^2/a^2}$ .
5. Find the centroid of the triangle whose sides have equations  $y = 6 - x$ ,  $y = 6 + 3x$ , and  $x = 5$ .